3 POINTS FOR EACH PROBLEM

1.	Contest Math Ka	angaroo takes	s place in	Europe	every y	vear since	e 1991.	In year	2006 it	will	be t	he
	contest.											

A)	15^{th}	B) 16^{th}	C) 17^{th}	D) 13^{th}	E) 14^{th}
2.	$20 \times (0+6) - (20)$	$(\times 0) + 6 =$			
A)	0	B) 106	C) 114	D) 126	E) 12
3. Dei	Point O is the c atagon is the shade	enter of the regular pe d region?	entagon. What part o	f the whole	

A) 10% B) 20% C) 25% D) 30% <u>E) 40%</u>

4. Two sides of a triangle are 120 and 130 inches long. Which of the following numbers below could not be the length of the third side of the triangle?

A) 40 B) 99 C) 100 D) 150 E) 260

5. 2006 students participated in a survey. The survey stated that 1500 of them participated in the Math Kangaroo Contest, and 1200 of them participated in an English Language Contest. Out of the students who participated in the survey, how many participated in both contests if it's known that 6 people did not take part in any of the competitions?

A) 300 B) 500 C) 600 D) 700 E) 1000

6. A solid is made out of two cubes with edges 1 inch and 3 inches. What is the surface area of the solid in square inches?

A) 56 B) 58 C) 59 D) 60 E) 64



7. A bottle of a volume of $\frac{1}{3}$ liter is $\frac{3}{4}$ filled with juice. How much juice will be left in the bottle after pouring out $\frac{1}{5}$ of a liter?

A) $\frac{1}{20}$ liter B) $\frac{3}{40}$ liter C) 0,13 liter D) $\frac{1}{8}$ liter E) The bottle will be empty.

8. Out of isosceles triangles with sides of 7, and a base with the length expressed by whole number, the triangle with the greatest perimeter was selected. This perimeter is equal to:

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9. Granny baked dumplings for her grandchildren. If she gave each one of them 2 dumplings, she would still have 3 more left, but if she gave each one of them 3 dumplings, she would be short by two. How many grandchildren does she have?

A) 2 B) 3 C) 4 D) 5 E) 6

10. Out of which figure below can you make the box shown in the picture?



4 POINTS FOR EACH PROBLEM

11. How many non-negative whole numbers smaller than 100 can you get as a sum of nine consecutive whole numbers?

A) 13 B) 12 C) 11 D) 10 E) 9

12. In some month three Tuesdays came out to be on even days of the month. Which day of the week will be the 21st day of that month?

13. Mark, Matthew, and Peter were saving money to buy a tent. Mark had 60% of the needed sum, and Matthew gave 40% of the remaining amount. Peter gave 30 dollars to complete the sum. How much was the tent?

A) \$50 B) \$60 C) \$125 D) \$150 E) \$200

14. A group of aliens was traveling in a spaceship. Each one of them was dressed in a jumpsuit that was of one of the following colors: green, orange, or blue. Each alien dressed in a green jumpsuit had two tentacles, each alien dressed in an orange suit had three tentacles, and each alien dressed in a blue jumpsuit had five tentacles. There were as many aliens dressed in green suits as those dressed in orange, and there were 10 more aliens dressed in blue than those dressed in green. All aliens together had 250 tentacles. How many aliens were dressed in blue?

15. When Jumpy, the Kangaroo, jumps on his left foot his jump is 2 feet long and when he jumps on his right foot then his jump is 4 feet long. If Jumpy jumps using his both feet, then his jumps are 7 feet long. What is the smallest number of jumps that Jumpy must make to travel exactly 1000 feet?

A) 140 B) 144 C) 175 D) 176 E) 150

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20. The digit of ones of a certain three-digit number is 2. If we move this digit to the beginning of that number, as a result we will get a three digit number that is smaller than the original one by 36. What is the sum of the digits of that number?

A)	1 B) 10 C) 7 D)) 9 E)	5
		/	, , , , , , , , , , , , , , , , , , , ,	/	

5 POINTS FOR EACH PROBLEM

21.	Helen drew a 5×5 -square and marked centers of each small square	A_{\Box}							
After	erwards, she drew obstacles and then she tested in how many ways i	it 🔁	•	•	•	•	•		
was	possible to move from A to B in the shortest possible way avoid in	g	•	•	•	•	•		
the o	obstacles, and moving vertically or horizontally from center to center	r .	•	•	•	•	•		
of ea	ach small square. How many possible paths of the sho rtest length ar	e	•	•	•	•	•		
there	re?		•	•	•	•	•	B	
A) 6	6 B) 8 C) 9 D) 11 E) 1	2				1]	D	
22. A train consists of a locomotive and five cars marked I, II, III, IV and V. In how many ways can you rearrange the cars, in such way that car I is always closer to the locomotive than car II?									
A) 1	120 B) 60 C) 48 D)	30				I	E)	10	
23.	What is the first digit of the smallest natural number that sum of i	ts digits e	equ	als	20)06'	?		

A) 1 B) 3 C) 5 D) 6 E) 8

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24. How many isosceles triangles with area of 1 have a side with it's length equal to 2?

A) 0 B) 1 C) 2 D) 3 E) 4

25. Peter rides a bicycle from town P to town Q with a constant speed. If he increases his speed by 3 m/s, he will arrive to town Q 3 times faster. How many times faster will Peter arrive to town Q, if he increases his speed by 6 m/s?

A) 4 B) 5 C) 6 D) 4.5 E) 8

26. If the product of two integers equals $2^5 \cdot 3 \cdot 5^2 \cdot 7^3$, then their sum can be:

- A) divisible by 8.
- C) divisible by 5.

A) 96

E) Cannot be divided by any of numbers: 8, 3, 5, 49.



28. The first row shows 11 cards, each with 2 letters. The second row shows rearrangement of the cards from the first row. Which of the following could appear on the bottom line of the second row?



A) ANJAMKILIOR D) RAONJMILIKA B) RLIIMKOJNAA

C) JANAMKILIRO E) ANMAIKOLIRJ

29. What is the value of this expression:

	$(1^2 + 2^2 + 3^2 + \ldots + 2005^2)$	$) - (1 \times 3 + 2 \times 4 + 3)$	$(5 + \ldots + 2004 \times 2006)?$	
A) 2000	B) 2004	C) 2005	D) 2006	E) 0

30. Let x, y, and z be positive real numbers and let $x \ge y \ge z$ so that x + y + z = 20.1. Which of the following statements is true?

A) Always xy < 99. B) Always xy > 1. C) Always $xy \neq 75$. D) Always $xy \neq 25$. E) None of the statements is true.

DCР R

R



B) divisible by 3.